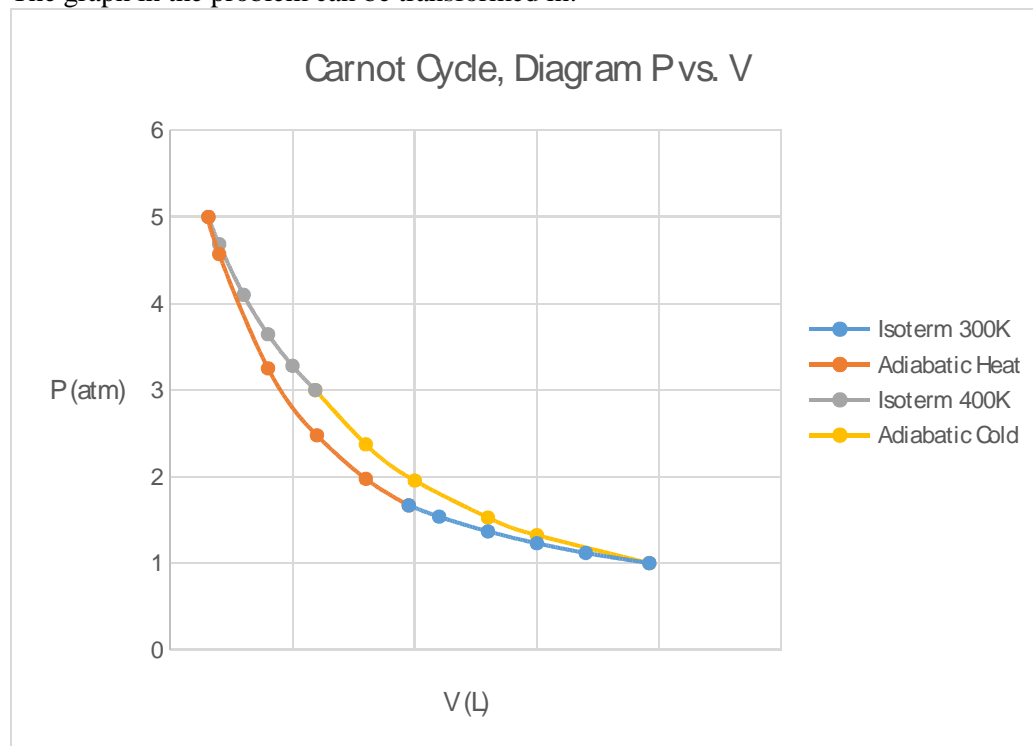


Problem 3 Carnot cycle

The graph in the problem can be transformed in:



3.1

In the isothermal compression:

$$\Delta U = 0 \quad W = -nRT \cdot \ln(V_f/V_i) = -nRT \cdot \ln(P_i/P_f) = -n \cdot 8.314 \cdot 300 \cdot \ln(1/1.6667) = 1274.15n \text{ J}$$

$$Q = -1274.15n \text{ J}$$

In the adiabatic compression:

$$Q = 0 \quad \Delta E = nC_v \cdot (T_f - T_i) = 100n \cdot C_v \quad W = 100n \cdot C_v$$

In the isothermal expansion:

$$\Delta U = 0 \quad W = -nRT \cdot \ln(V_f/V_i) = -nRT \cdot \ln(P_i/P_f) = -n \cdot 8.314 \cdot 400 \cdot \ln(5/3) = -1698.8n \text{ J}$$

$$Q = 1698.8n \text{ J}$$

In the adiabatic expansion:

$$Q = 0 \quad \Delta E = nC_v \cdot (T_f - T_i) = -100n \cdot C_v \quad W = -100n \cdot C_v$$

Useful work in the cycle = -424.65 n J. The work is not defined because the number of mol is missing.

3.2

The efficiency η is defined, $\eta = (\text{useful work})/(\text{heat given}) = (424.65n)/(1698.8n) = 0.25$

Even the efficiency $\eta = 1 - (T_{\text{cold}}/T_{\text{heat}}) = 1 - (300/400) = 0.25$

3.3

In the adiabatic compression:

$$P_{\text{initial}} = 1.6667 \quad V_{\text{initial}} = nR(300)/1.6667$$

$$P_{\text{final}} = 5 \quad V_{\text{final}} = nR(400)/5$$

The relation $PV^\gamma = \text{const}$ is true.

Then:

$$1.6667 \cdot (nR(300)/1.6667)^\gamma = 5 \cdot (nR(400)/5)^\gamma$$

$$\{(300 \times 5)/(400 \times 1.6667)\}^\gamma = (5/1.6667)$$

$$2.25^\gamma = 3$$

$$\gamma = 1.355 = 1 + R/C_v \quad C_v = 5.634R/2$$

3.4

The C_v founded not correspond with C_v for monoatomic, diatomic or triatomic gas.

Solution proposed by

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